## 15. This Way to Infinity

Into the cavern rushed eight of the strongest miners carrying an immense caldron which bubbled and sizzled and sent great clouds of savoury steam spiralling slowly to the ceiling. A sweet yet pungent aroma hung in the air and drifted easily from one anxious nose to the other, stopping only long enough to make several mouths water and a few stomachs growl. Milo, Tock, and the Humbug watched eagerly as the rest of the workers put down their tools and gathered around the big pot to help themselves.
"Perhaps you'd care for something to eat?" asked the Mathemagician, offering each of them a heaping bowlful.
"Yes, sir," said Milo, who was beside himself with hunger.
"Thank you," added Tock.
The Humbug made no reply, for he was already too busy eating and, in a moment, the three of them had finished absolutely everything they'd been given.
"Please have another portion," said the Mathemagician, filling their bowls once more and, as quickly as they'd finished the first one, the second was emptied, too.
"Don't stop now," he insisted, serving them again, and again, and again, and again, and again. "How very strange," thought Milo, as he finished his seventh helping. "Each one I eat makes me a little hungrier than the one before.
"Do have some more," suggested the Mathemagician, and they continued to eat just as fast as he filled their plates.
After Milo had eaten nine portions, Tock eleven, and the Humbug, without once stopping to look up, twenty-three, the Mathemagician blew his whistle for a second time and immediately the pot was removed and the miners returned to work.
"U-g-g-g-h-h-h," gasped the bug, suddenly realising that he was twenty-three times hungrier than when he started, "I think I'm starving."
"Me, too," complained Milo, whose stomach felt as empty as he could ever remember; "and I ate so much."
"Yes, it was delicious, wasn't it?" agreed the pleased Dodecahedron, wiping the gravy from several of his mouths. "It's the specialty of the kingdom-subtraction stew."
"I have more of an appetite than when I began," said Tock, leaning weakly against one of the larger rocks.
"Certainly," replied the Mathemagician; "what did you expect? The more you eat, the hungrier you get. Everyone knows that."
"They do?" said Milo doubtfully. "Then how do you ever get enough?"
"Enough?" he said impatiently. "Here in Digitopolis we have our meals when we're full and eat until we're hungry. That way, when you don't have anything at all, you have more than enough. It's a very economical system. You must have been quite stuffed to have eaten so much."
"It's completely logical," explained the Dodecahedron. "The more you want, the less you get, and the less you get, the more you have. Simple arithmetic, that's all. Suppose you had something and added something to it. What would that make?"
"More," said Milo quickly.
"Quite correct," he nodded. "Now, suppose you had something and added nothing to it. What would you have?"
"The same," he answered again, without much conviction.
"Splendid," cried the Dodecahedron. "And suppose you had something and added less than nothing to it. What would you have then?"
"FAMINE!" roared the anguished Humbug, who suddenly realised that that was exactly what he'd eaten twenty-three bowls of.
"It's not as bad as all that," said the Dodecahedron from his most sympathetic face. "In a few hours you'll be nice and full again-just in time for dinner."
"Oh dear," said Milo sadly and softly. "I only eat when I'm hungry."
"What a curious idea," said the Mathemagician, raising his staff over his head and scrubbing the rubber end back and forth several times on the ceiling. "The next thing you'll have us believe is that you only sleep when you're tired." And by the time he'd finished the sentence, the cavern, the miners, and the Dodecahedron had vanished, leaving just the four of them standing in the Mathemagician's workshop.
"I often find," he casually explained to his dazed visitors, "that the best way to get from one place to another is to erase everything and begin again. Please make yourself at home."
"Do you always travel that way?" asked Milo as he glanced curiously at the strange circular room, whose sixteen tiny arched windows corresponded exactly to the sixteen points of the compass. Around the entire circumference were numbers from zero to three hundred and sixty, marking the degrees of the circle, and on the floor, walls, tables, chairs, desks, cabinets, and ceiling were labels showing their heights, widths, depths, and distances to and from each other. To one side was a gigantic note pad set on an artist's easel, and from hooks and strings hung a collection of scales, rulers, measures, weights, tapes, and all sorts of other devices for measuring any number of things in every possible way.
"No indeed," replied the Mathemagician and, this time, he raised the sharpened end of his staff, drew a thin straight line in the air, and then walked gracefully across it from one side of the room to the other. "Most of the time, I take the shortest distance between any two points. And, of course, when I should be in several places at once," he remarked, writing 7 X $1=7$ carefully on the note pad, "I simply multiply."
Suddenly there were seven Mathemagicians standing side-by-side, and each one looked exactly like the other.
"How did you do that?" gasped Milo.
"There's nothing to it," they all said in chorus, "if you have a magic staff." Then six of them cancelled themselves out and simply disappeared.
"But it's only a big pencil," the Humbug objected, tapping at it with his cane.
"True enough," agreed the Mathemagician; "but once you learn how to use it, there's no end to what you can do."
"Can you make things disappear?" asked Milo excitedly.
"Why, certainly," he said, striding over to the easel. "Just step a little closer and watch carefully."
After demonstrating that there was nothing up his sleeves, in his hat, or behind his back, he wrote quickly:

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4+9-2 \times 16+1 / 3 \times 6-67+8 \times 2-3+26-1 / 34+3 / 7+2-5=
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Then he looked up expectantly.
"Seventeen!" shouted the bug, who always managed to be first with the wrong answer.
"It all comes to zero," corrected Milo.
"Precisely," said the Mathemagician, making a very theatrical bow, and the entire line of numbers vanished before their eyes. "Now, is there anything else you'd like to see?"
"Yes, please," said Milo. "Can you show me the biggest number there is?"
"I'd be delighted," he replied, opening one of the closet doors. "We keep it right here. It took four miners just to dig it out."
Inside was the biggest three Milo had ever seen. It was fully twice as high as the Mathemagician.
"No, that's not what I mean," objected Milo. "Can you show me the longest number there is?" "Surely," said the Mathemagician, opening another door. "Here it is. It took three carts to carry it here."

Inside this closet was the longest eight imaginable. It was just about as wide as the three was high.
"No, no, no, that's not what I mean either," he said, looking helplessly at Tock.
"I think what you would like to see," said the dog, scratching himself just under half-past four, "is the number of greatest possible magnitude."
"Well, why didn't you say so?" said the Mathemagician, who was busily measuring the edge of a raindrop. "What's the greatest number you can think of?"
"Nine trillion, nine hundred ninety-nine billion, nine hundred ninety-nine million, nine hundred ninety-nine thousand, nine hundred ninety-nine," recited Milo breathlessly.
"Very good," said the Mathemagician. "Now, add one to it. Now, add one again," he repeated when Milo had added the previous one. "Now, add one again. Now, add one again. Now, add one again. Now, add one again. Now, add one again. Now, add one again. Now, add... " "But when can I stop?" pleaded Milo.
"Never," said the Mathemagician with a little smile, "for the number you want is always at least one more than the number you've got, and it's so large that if you started saying it yesterday you wouldn't finish tomorrow."
"Where could you ever find a number so big?" scoffed the Humbug.
"In the same place they have the smallest number there is," he answered helpfully; "and you know what that is."
"Certainly," said the bug, suddenly remembering something to do at the other end of the room.
"One one-millionth?" asked Milo, trying to think of the smallest fraction possible.
"Almost," said the Mathemagician. "Now, divide it in half. Now, divide it in half again. Now, divide it in half again. Now, divide it in half again. Now, divide it in half again. Now, divide it in half again. Now, divide... "
"Oh dear," shouted Milo, holding his hands to his ears, "doesn't that ever stop either?"
"How can it," said the Mathemagician, "when you can always take half of whatever you have left until it's so small that if you started to say it right now, you'd finish even before you began?"
"Where could you keep anything so tiny?" Milo asked, trying very hard to imagine such a thing.
The Mathemagician stopped what he was doing and explained simply, "Why, in a box that's so small you can't see it and that's kept in a drawer that's so small you can't see it, in a dresser that's so small you can't see it, in a house that's so small you can't see it, on a street that's so small you can't see it, in a city that's so small you can't see it, which is part of a country that's so small you can't see it, in a world that's so small you can't see it."
Then, he sat down, fanned himself with a handkerchief, and continued. "Then, of course, we keep the whole thing in another box that's so small you can't see it-and, if you follow me, I'll show you where to find it."

They walked to one of the small windows and there, tied to the sill, was one end of a line that stretched along the ground and into the distance until completely out of sight.
"Just follow that line forever," said the Mathemagician, "and, when you reach the end, turn left. There you'll find the land of Infinity, where the tallest, the shortest, the biggest, the smallest, and the most and the least of everything are kept."
"I really don't have that much time," said Milo anxiously. "Isn't there a quicker way?"
"Well, you might try this flight of stairs," he suggested, opening another door and pointing up. "It goes there, too."
Milo bounded across the room and started up the stairs two at a time. "Wait for me, please," he shouted to Tock and the Humbug. "I'll be gone just a few minutes.

